

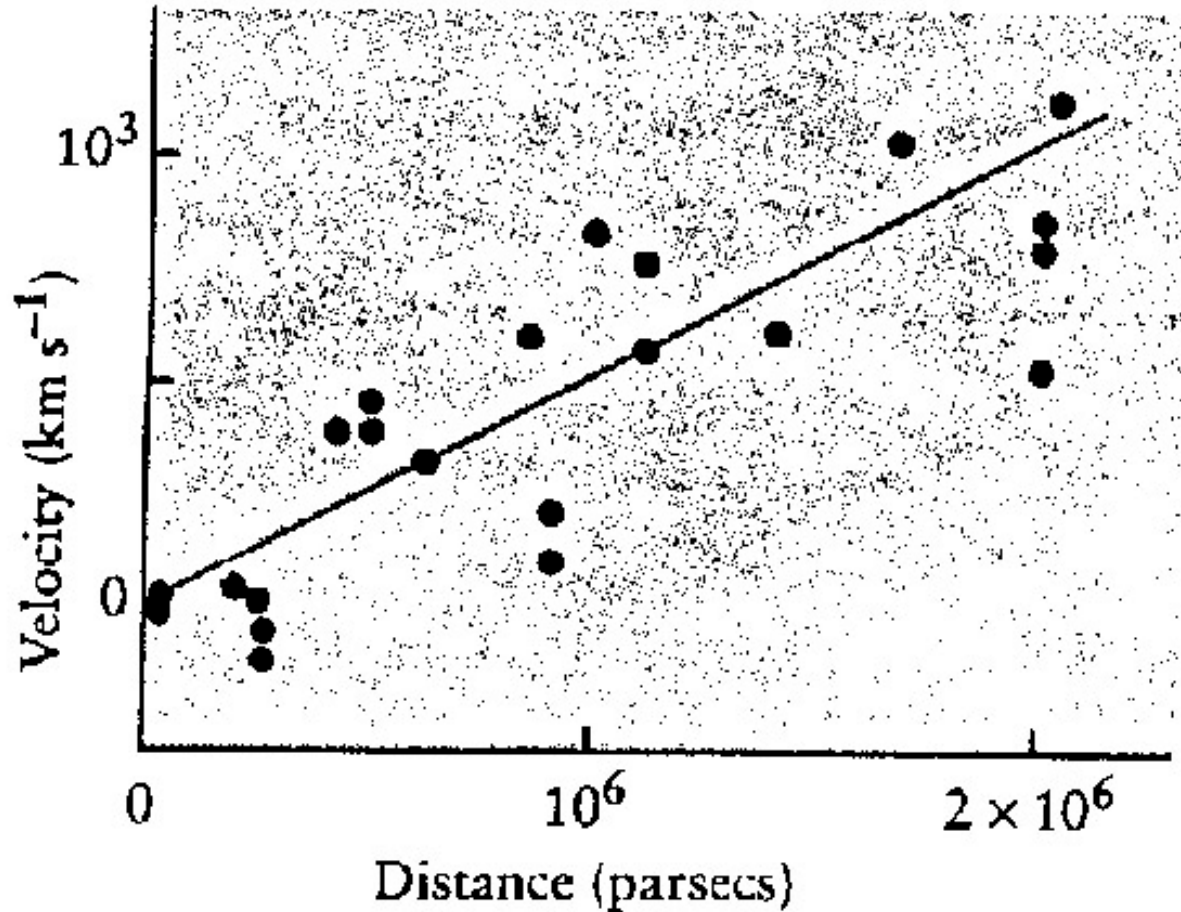
# Reducing the $H_0$ Tension with Exponential Acoustic Dark Energy

Lu Yin

CQeST  
Sogang University



# The discovery of Hubble constant



$$v = H_0 \times D$$

E. Hubble, Proc. Nat. Acad. Sci. 15 (1929), 168-173



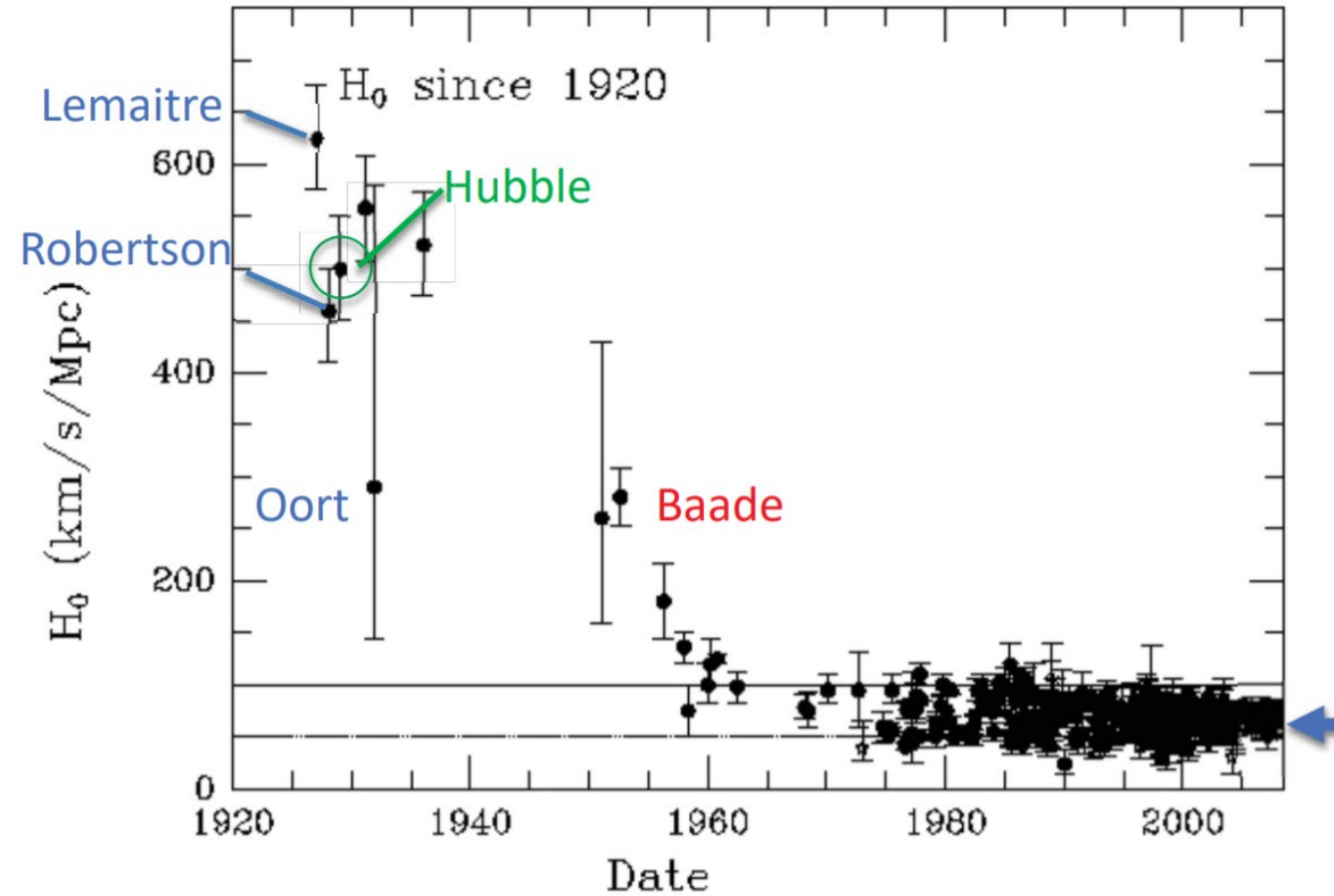
Edwin Hubble

$V$  : recessional velocity

$D$  : the proper distance to the observer

$H_0$  : Hubble's constant [km/s/Mpc]

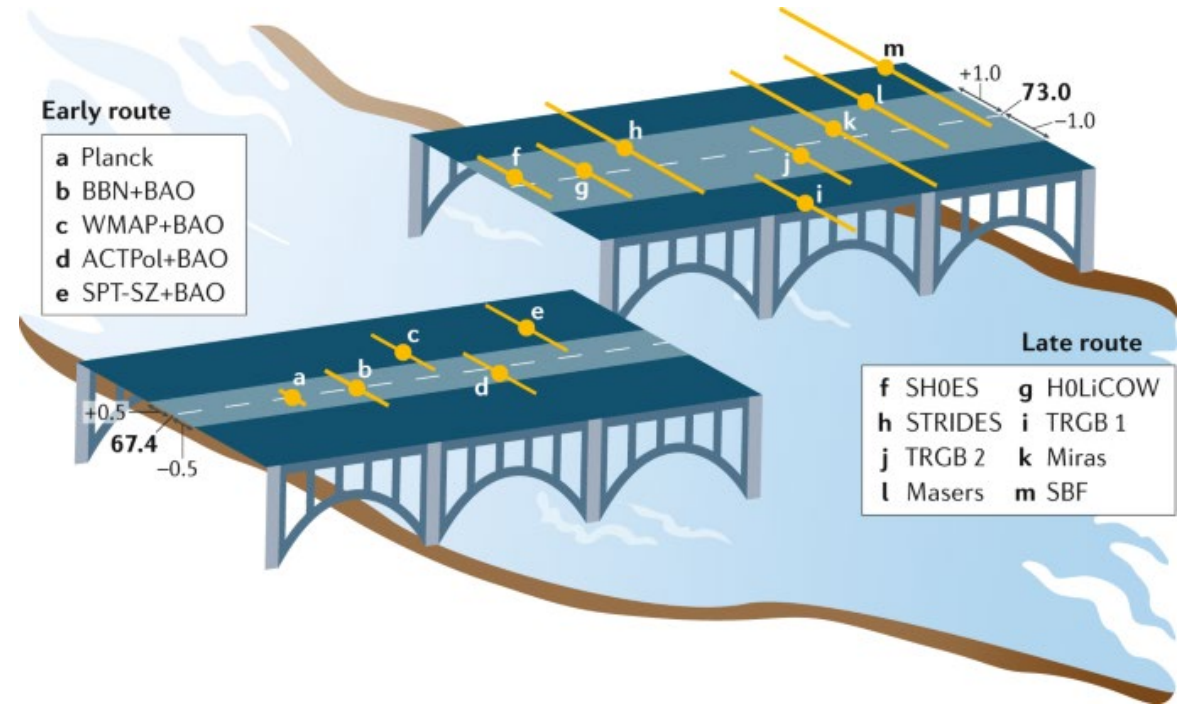
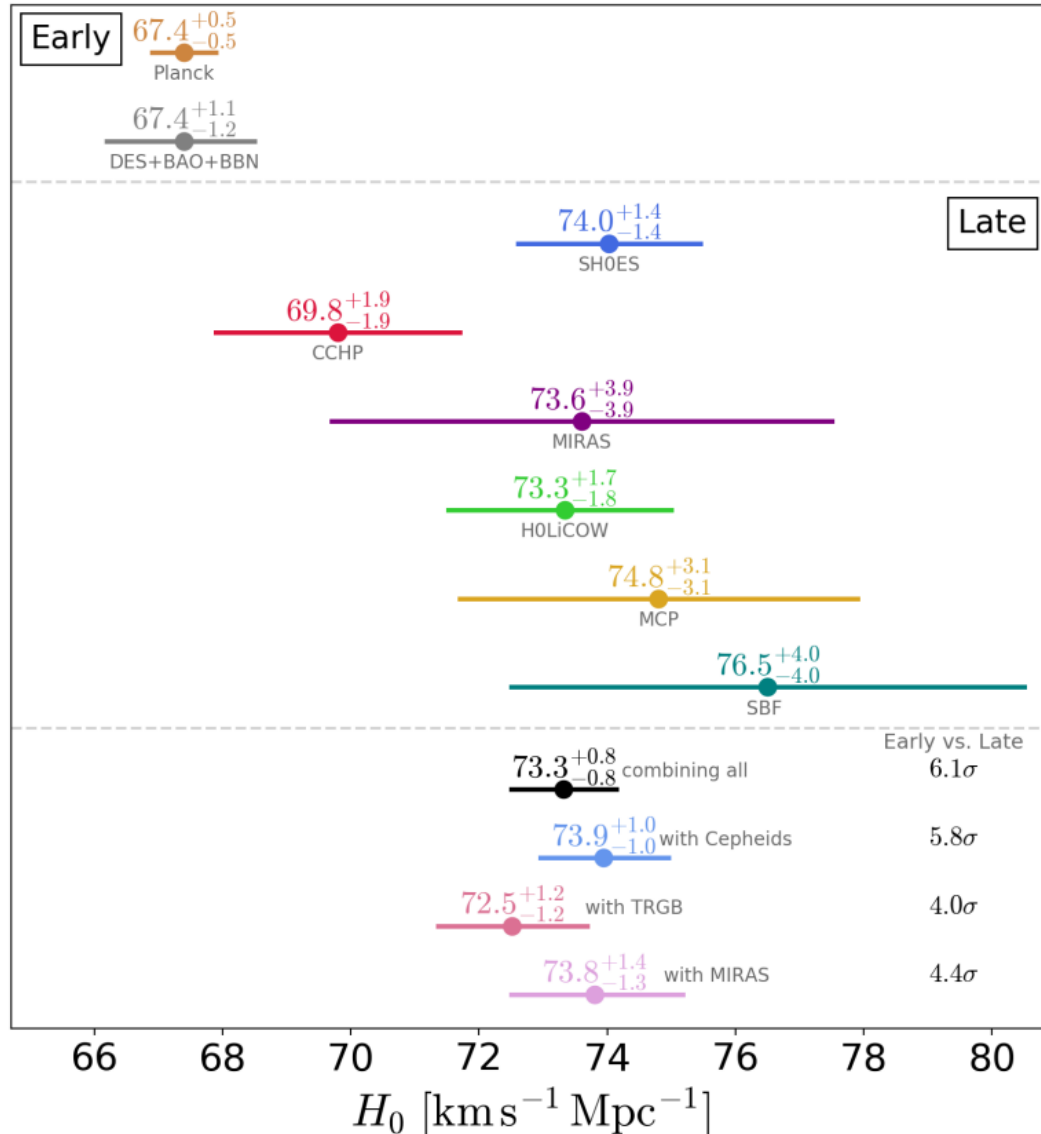
# History of the Hubble constant



Copyright J. Huchra 2008

# The $H_0$ tension

flat –  $\Lambda$ CDM



[ L. Verde, T. Treu and A. G. Riess *Nature Astron.* 3, 891 ]

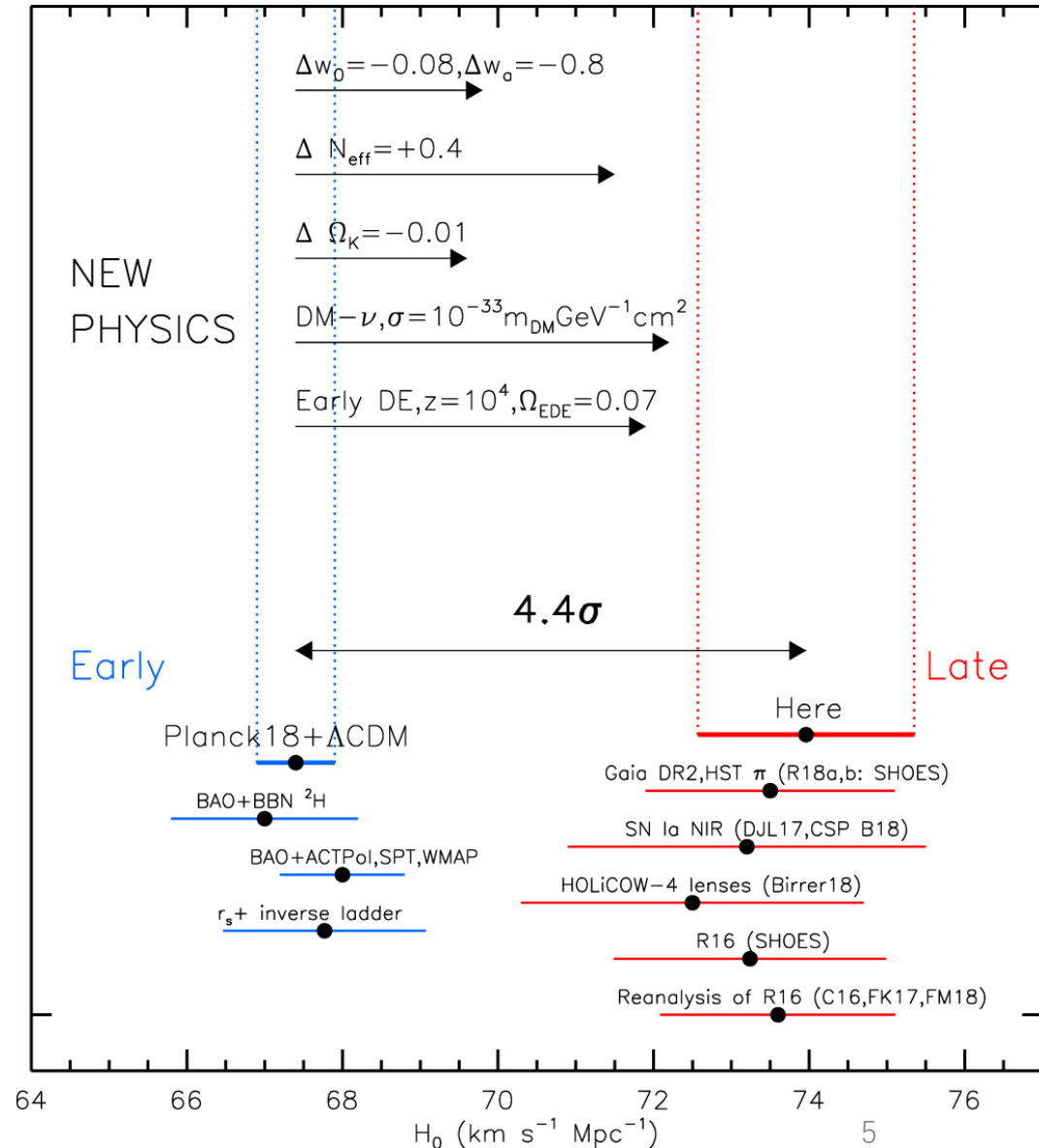
# Potential new physics beyond $\Lambda$ CDM

Another relativistic species  
(e.g., additional neutrino or dark radiation)

Non-zero spatial curvature

A decaying relic massive dark matter

Early dark energy



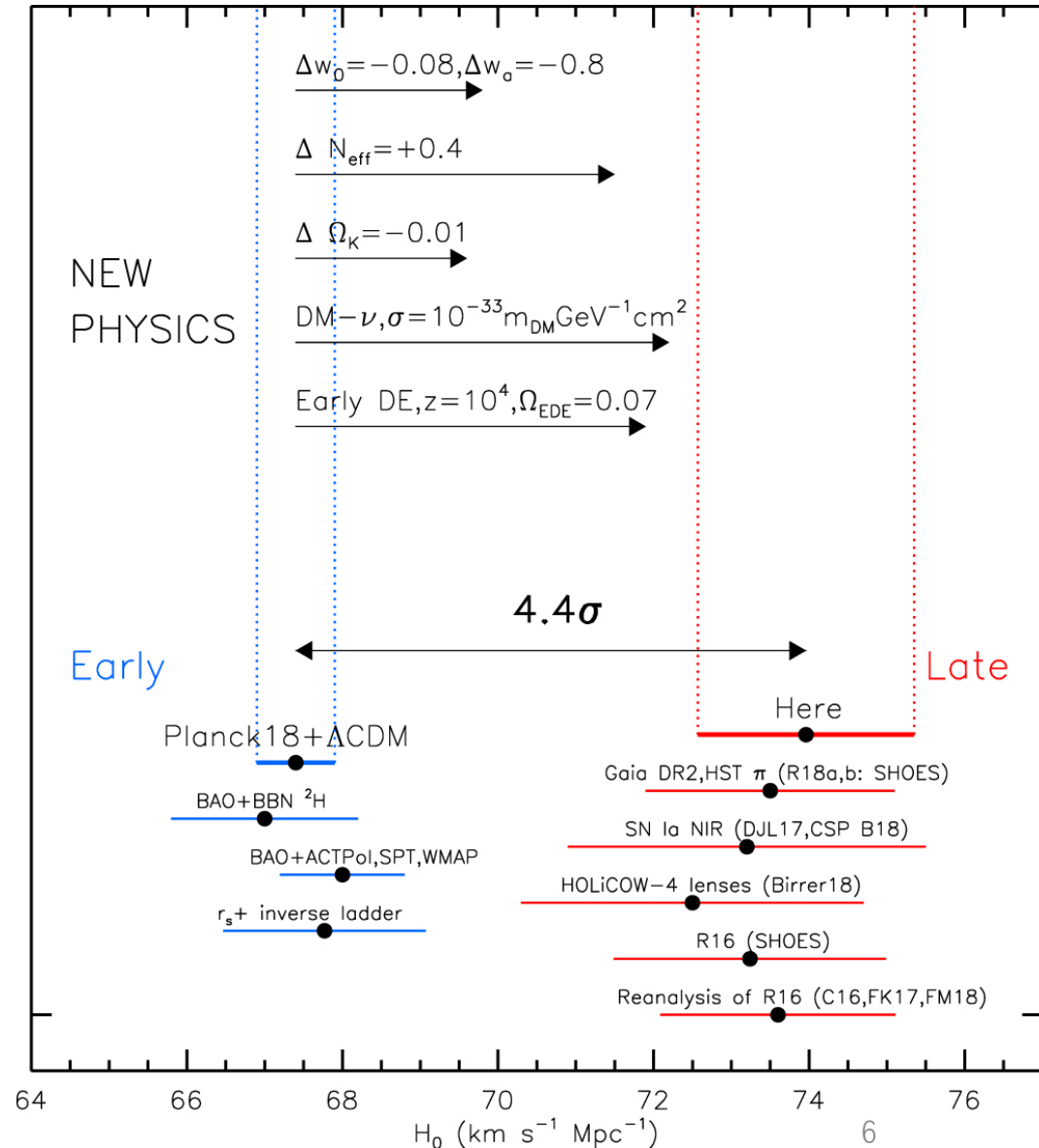
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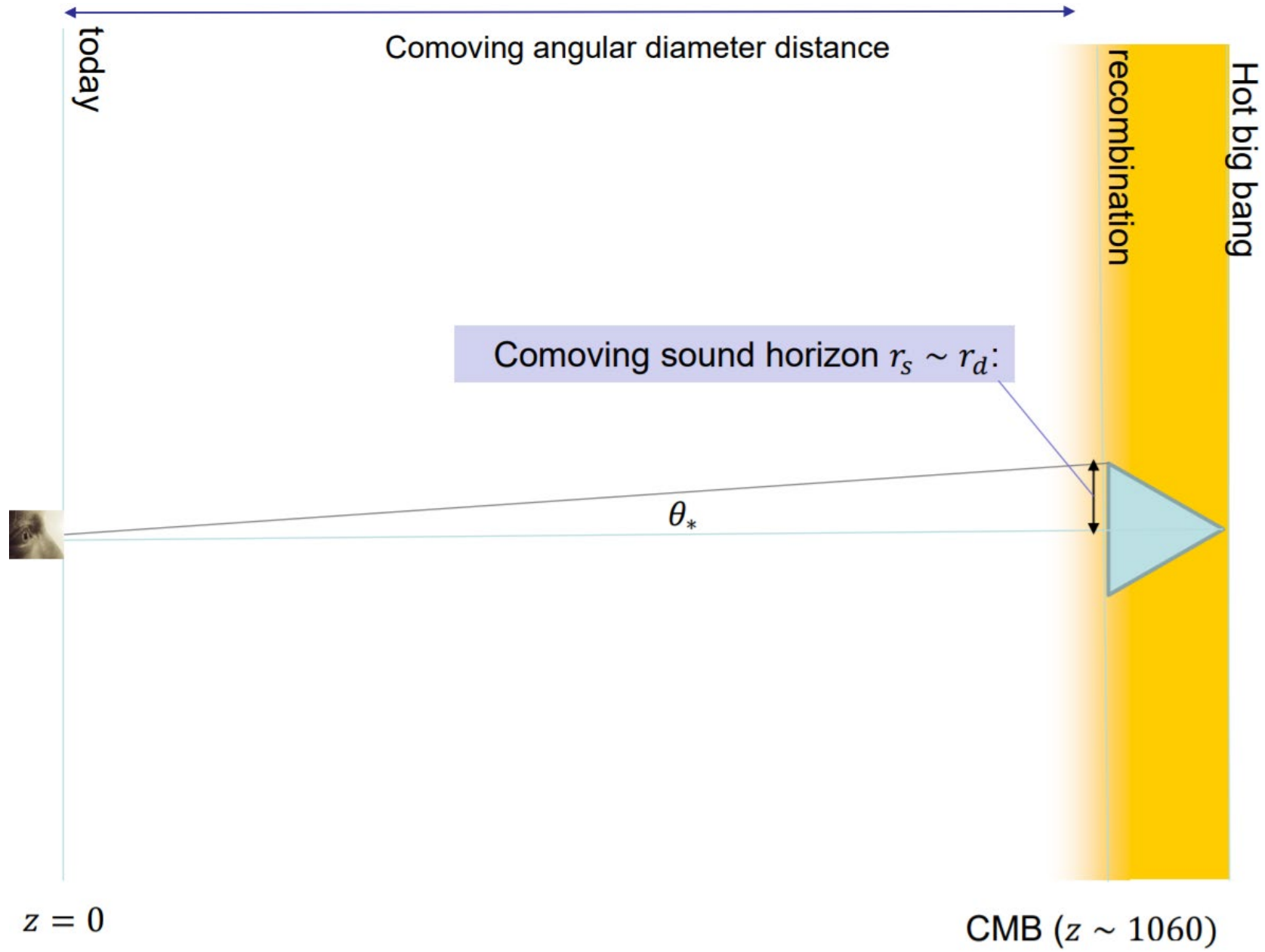
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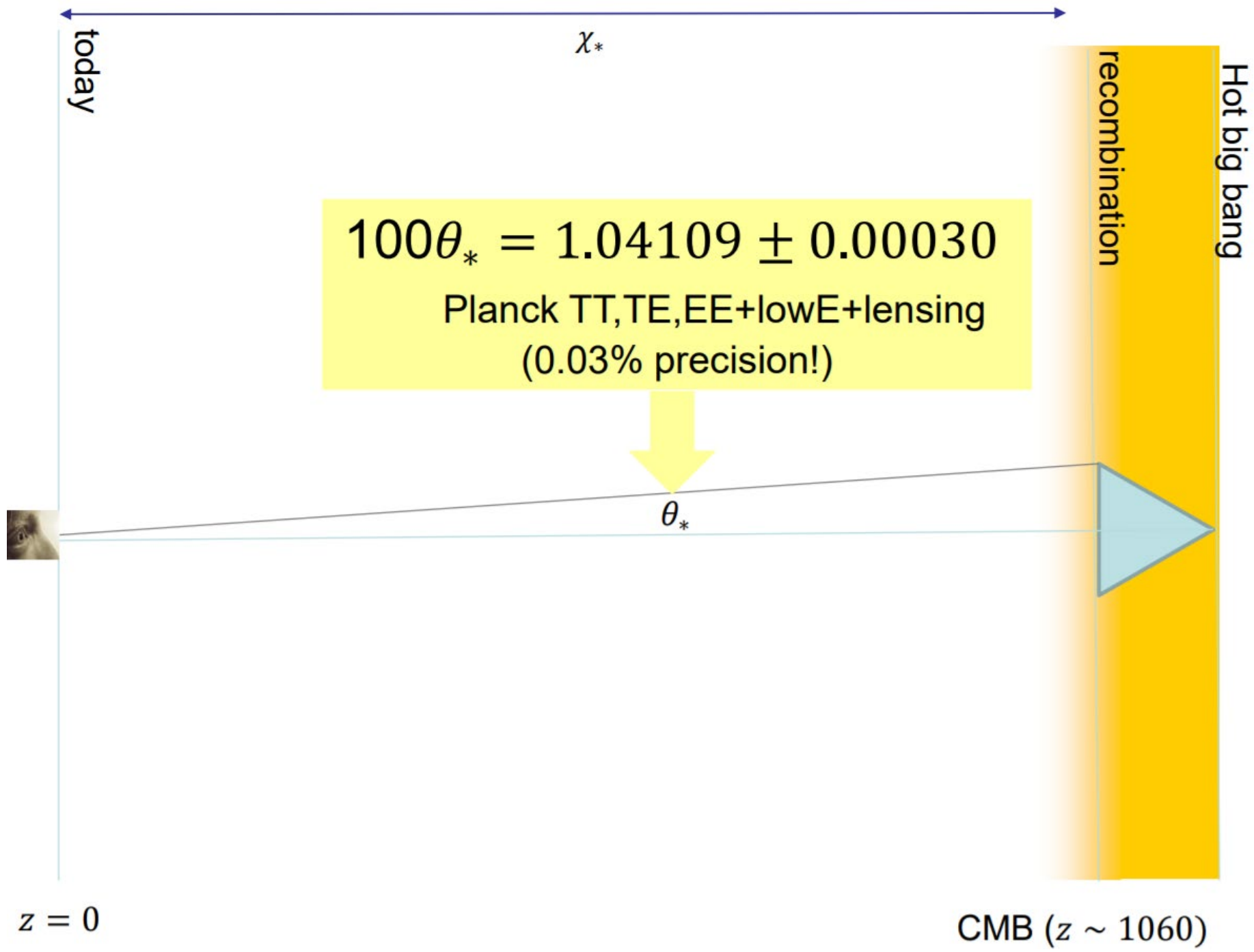
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Early dark energy

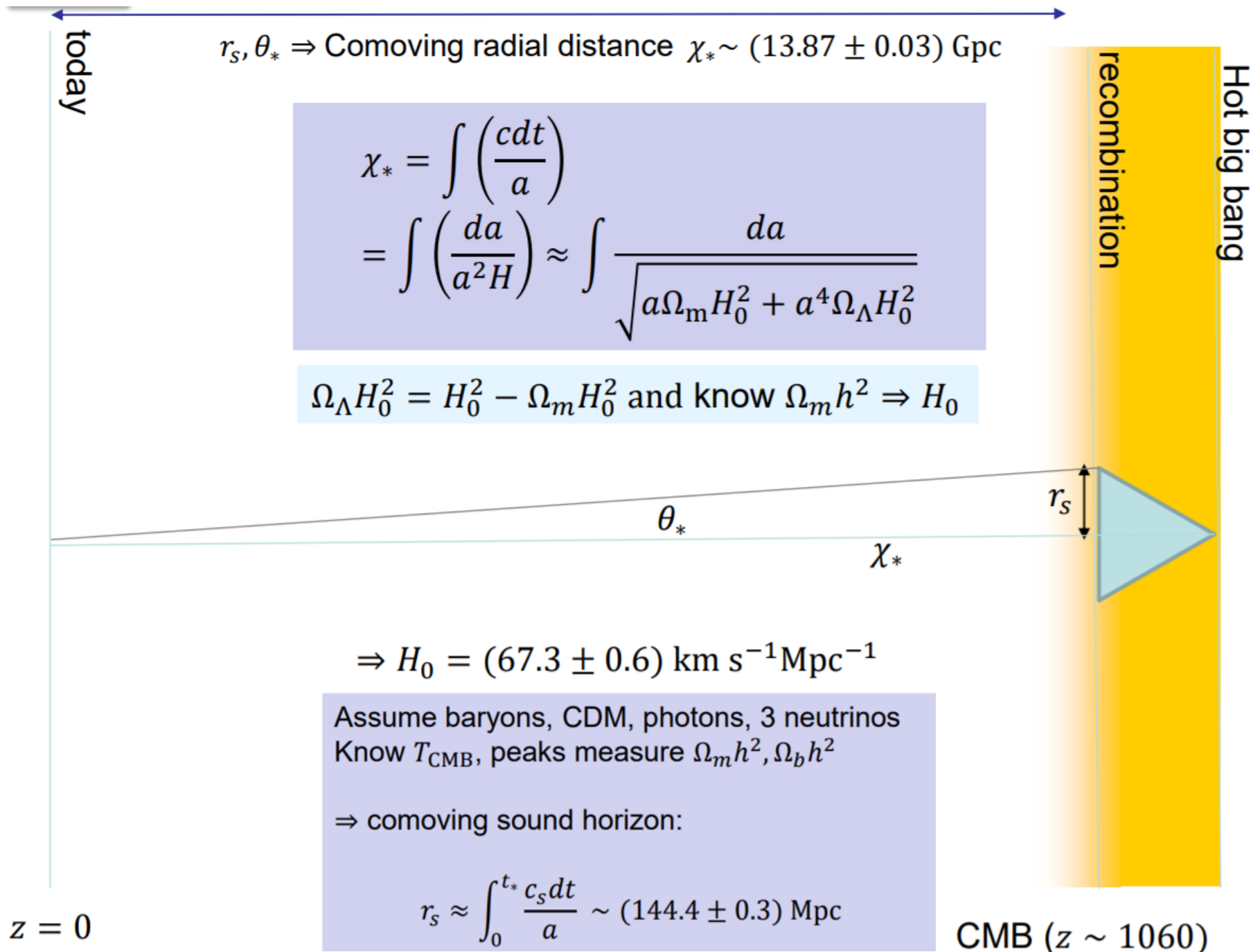


# $H_0$ from CMB and Planck









# In the Realm of the Hubble tension – a Review of Solutions †

Eleonora Di Valentino<sup>1\*</sup>, Olga Mena<sup>2</sup>, Supriya Pan<sup>3</sup>, Luca Visinelli<sup>4</sup>, Weiqiang Yang<sup>5</sup>, Alessandro Melchiorri<sup>6</sup>, David F. Mota<sup>7</sup>, Adam G. Riess<sup>8,9</sup>, Joseph Silk<sup>8,10,11</sup>

[ *Class.Quant.Grav.* 38 (2021) 15, 153001 ]

## 4 Early Dark Energy

- 4.1 Anharmonic Oscillations . . . . .
- 4.2 Ultra-Light Axions . . . . .
  - 4.2.1 Dissipative Axion: . . . . .
  - 4.2.2 Axion Interacting With a Dilaton: . . . . .
- 4.3 Power-Law Potential . . . . .
- 4.4 Rock ‘n’ Roll . . . . .
- 4.5 New Early Dark Energy . . . . .
- 4.6 Anti-de Sitter phase . . . . .
- 4.7 Graduated Dark Energy . . . . .
- 4.8 Acoustic Dark Energy . . . . .
  - 4.8.1 Exponential Acoustic Dark Energy: . . . . .
- 4.9 EDE in  $\alpha$ -attractors . . . . .

# The difference between EDE, ADE, eADE model

Early dark energy, the Hubble-parameter tension, and the string axiverse

Tanvi Karwal and Marc Kamionkowski  
*Department of Physics and Astronomy, Johns Hopkins University,  
3400 N. Charles St., Baltimore, MD 21218*  
(Dated: November 8, 2016)

$$w_\varphi(z) = \frac{1 + w_n}{1 + (a_c/a)^{3(1+w_n)}} - 1$$

$$w_n = (n - 1)/(n + 1)$$

$$n = 2 \quad | \quad n = 3 \quad | \quad n = \infty$$

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Acoustic Dark Energy: Potential Conversion of the Hubble Tension

Meng-Xiang Lin,<sup>1</sup> Giampaolo Benevento,<sup>2,3,1</sup> Wayne Hu,<sup>1</sup> and Marco Raveri<sup>1</sup>

<sup>1</sup>*Kavli Institute for Cosmological Physics, Department of Astronomy & Astrophysics,  
Enrico Fermi Institute, The University of Chicago, Chicago, IL 60637, USA*

<sup>2</sup>*Dipartimento di Fisica e Astronomia "G. Galilei",  
Università degli Studi di Padova, via Marzolo 8, I-35131, Padova, Italy*

<sup>3</sup>*INFN, Sezione di Padova, via Marzolo 8, I-35131, Padova, Italy*

$$w_{\text{ADE}}(a) = \frac{1 + w_f}{[1 + (a_c/a)^{3(1+w_f)/p}]^p} - 1$$

$$c_s^2 = w_f = 1$$

$$p = 1/2$$

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## Reducing the $H_0$ Tension with Exponential Acoustic Dark Energy

Lu Yin<sup>1,2,\*</sup>

<sup>1</sup>*Center for Quantum Spacetime, Sogang University, Seoul 04107, Korea*

<sup>2</sup>*Department of Physics, Sogang University, Seoul 04107, Korea*

$$w_{e\text{ADE}}(a) = 2^{1 - \frac{a_c}{2a}} - 1$$

The eADE have less additional parameters

# The difference between EDE, ADE, eADE model

Value of EoS	$a \ll a_c$	$a = a_c$	$a = 1$
$w_{eADE}$	-1	$\sqrt{2} - 1$	1
$w_{ADE}$	-1	$\sqrt{2} - 1$	1
$w_{EDE}$ with $n = 3$	-1	-1/4	1/2
$w_{EDE}$ with $n = 2$	-1	-1/3	1/3

$$w_\varphi(z) = \frac{1 + w_n}{1 + (a_c/a)^{3(1+w_n)}} - 1$$

$$w_{ADE}(a) = \frac{1 + w_f}{[1 + (a_c/a)^{3(1+w_f)/p}]^p} - 1$$

## Reducing the $H_0$ Tension with Exponential Acoustic Dark Energy

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$$w_{eADE}(a) = 2^{1 - \frac{a_c}{2a}} - 1$$

The eADE have less additional parameters

# Background evolution and linear perturbation for eADE

The eADE density evolves as

$$\Omega_{eADE}(a) = \frac{\rho_{eADE}}{\rho_{tot}} = 2f_c \frac{(c_s^2 + 1)^2 - (w_{eADE} + 1)^2}{(c_s^2 + 1)^2}$$

$$1 + w_{eADE}(a) = 2^{1 - \frac{a_c}{2a}}$$

$$f_c = \frac{\rho_{eADE}(a_c)}{\rho_{tot}(a_c)}$$

When the sound speed equal to 1:

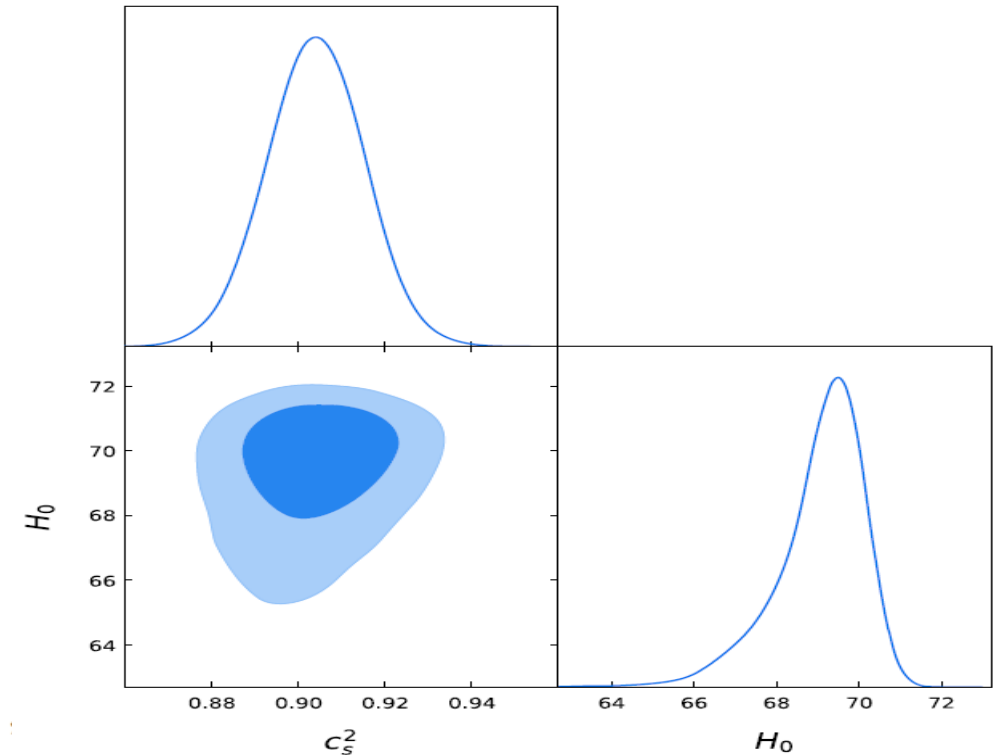
$$\Omega_{eADE}(a) \stackrel{c_s^2=1}{=} f_c \left[ 2 - \frac{(w_{eADE}(a) + 1)^2}{2} \right]$$

$$P_{eADE} \stackrel{c_s^2=1}{=} \frac{6H^2 f_c}{8\pi G} (-2\xi^3 + \xi^2 + 2\xi^1 - \xi^0) \quad \xi(a) = 2^{-\frac{a_c}{2a}}$$

The perturbation gives as:

$$\dot{\delta}_{eADE} = -(1 + w_{eADE})(\theta_{eADE} + \frac{\dot{h}}{2}) - 3\frac{\dot{a}}{a}(c_s^2 - w_{eADE})\delta_{eADE} - k\theta_{eADE},$$

$$\dot{\theta}_{eADE} = \frac{\dot{a}}{a}(2w_{eADE} - 1)\theta_{eADE} - \frac{\dot{w}_{eADE}}{1 + w_{eADE}}\theta_{eADE} + \frac{c_s^2 k^2}{a^2(1 + w_{eADE})}\delta_{eADE}$$



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$$1 + w_{eADE}(a) = 2^{1 - \frac{a_c}{2a}}$$

$$f_c = \frac{\rho_{eADE}(a_c)}{\rho_{tot}(a_c)}$$

When the sound speed equal to 1:

$$\Omega_{eADE}(a) \stackrel{c_s^2=1}{=} f_c \left[ 2 - \frac{(w_{eADE}(a) + 1)^2}{2} \right]$$

$$P_{eADE} \stackrel{c_s^2=1}{=} \frac{6H^2 f_c}{8\pi G} (-2\xi^3 + \xi^2 + 2\xi^1 - \xi^0)$$

	$n = 2$	$n = 3$	$n = \infty$
$f_{EDE}(a_c)$	0.028	0.050	0.054
$f_{ADE}(a_c)$	0.082		
$f_{eADE}(a_c)$	?		

The perturbation gives as:

$$\dot{\delta}_{eADE} = -(1 + w_{eADE})\left(\theta_{eADE} + \frac{\dot{h}}{2}\right) - 3\frac{\dot{a}}{a}(c_s^2 - w_{eADE})\delta_{eADE} - k\theta_{eADE},$$

$$\dot{\theta}_{eADE} = \frac{\dot{a}}{a}(2w_{eADE} - 1)\theta_{eADE} - \frac{\dot{w}_{eADE}}{1 + w_{eADE}}\theta_{eADE} + \frac{c_s^2 k^2}{a^2(1 + w_{eADE})}\delta_{eADE},$$



# Fitting result for the EDE and ADE model

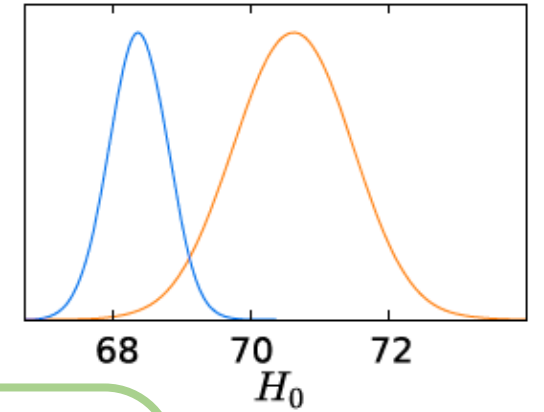
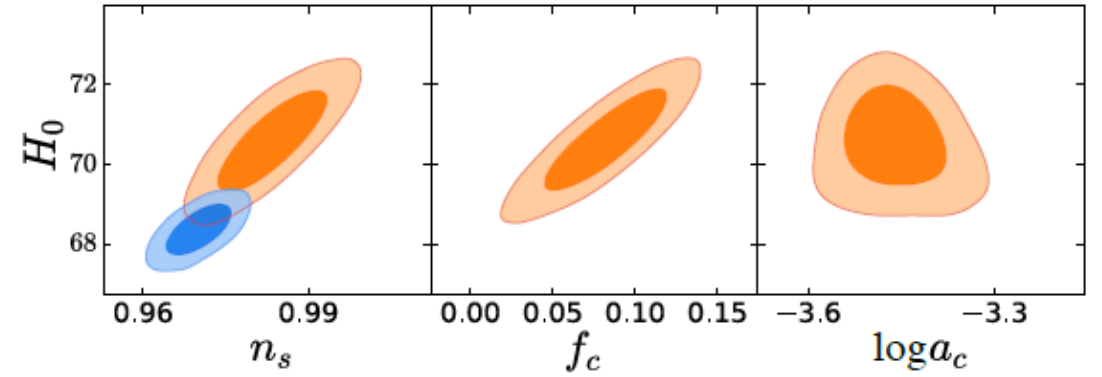
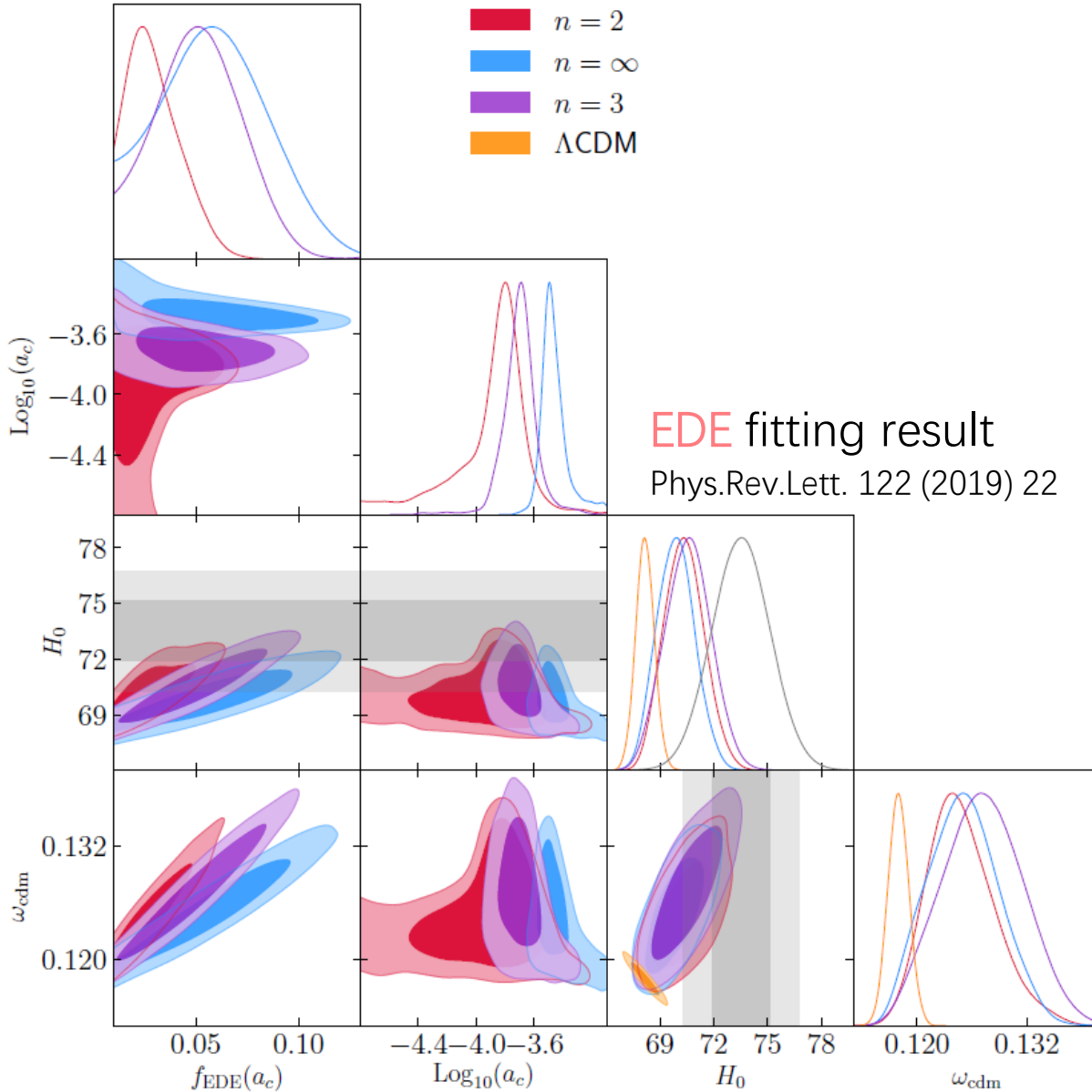
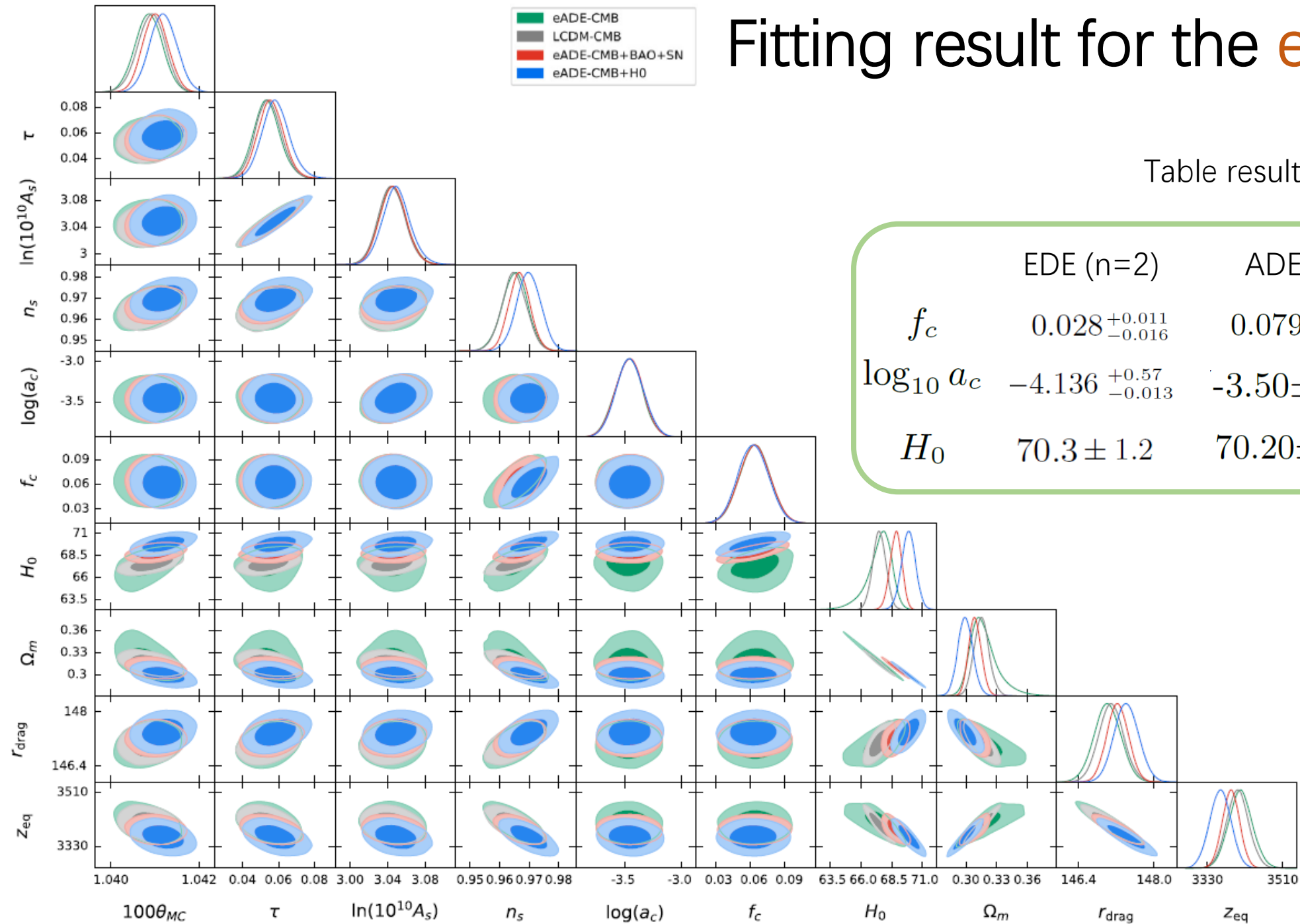


Table result

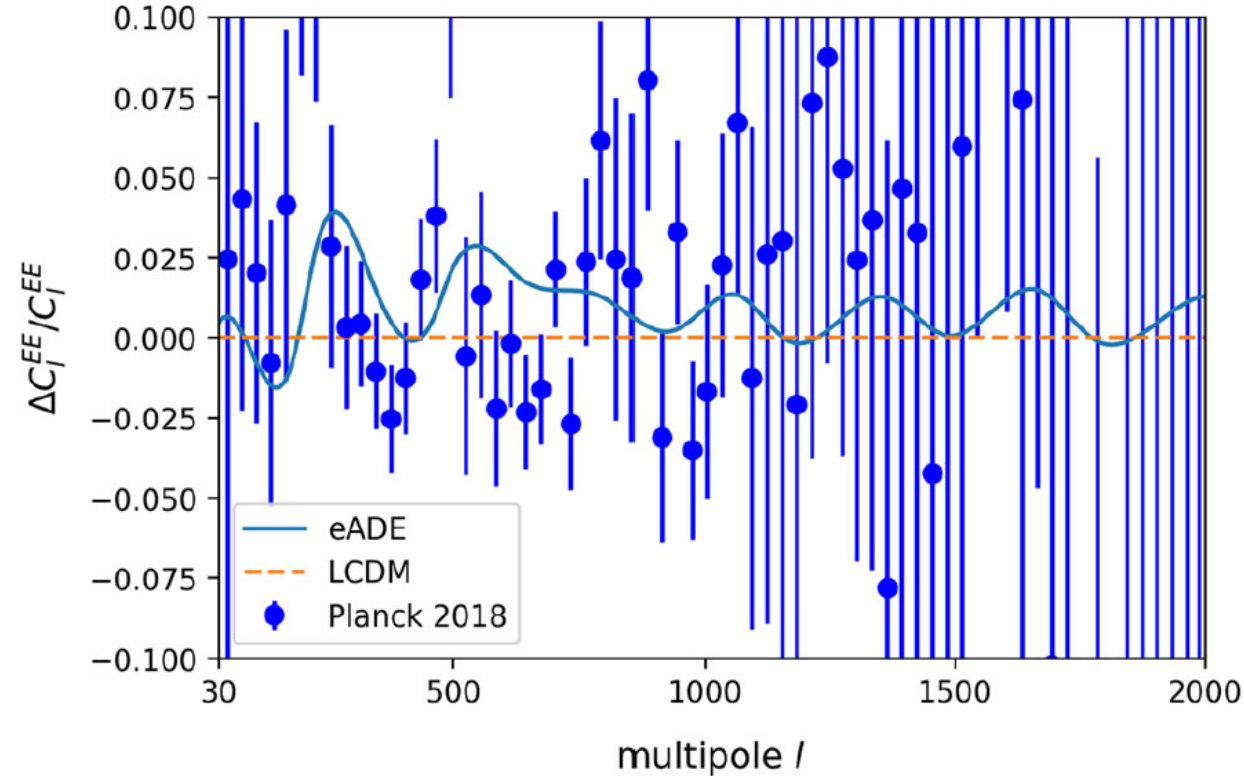
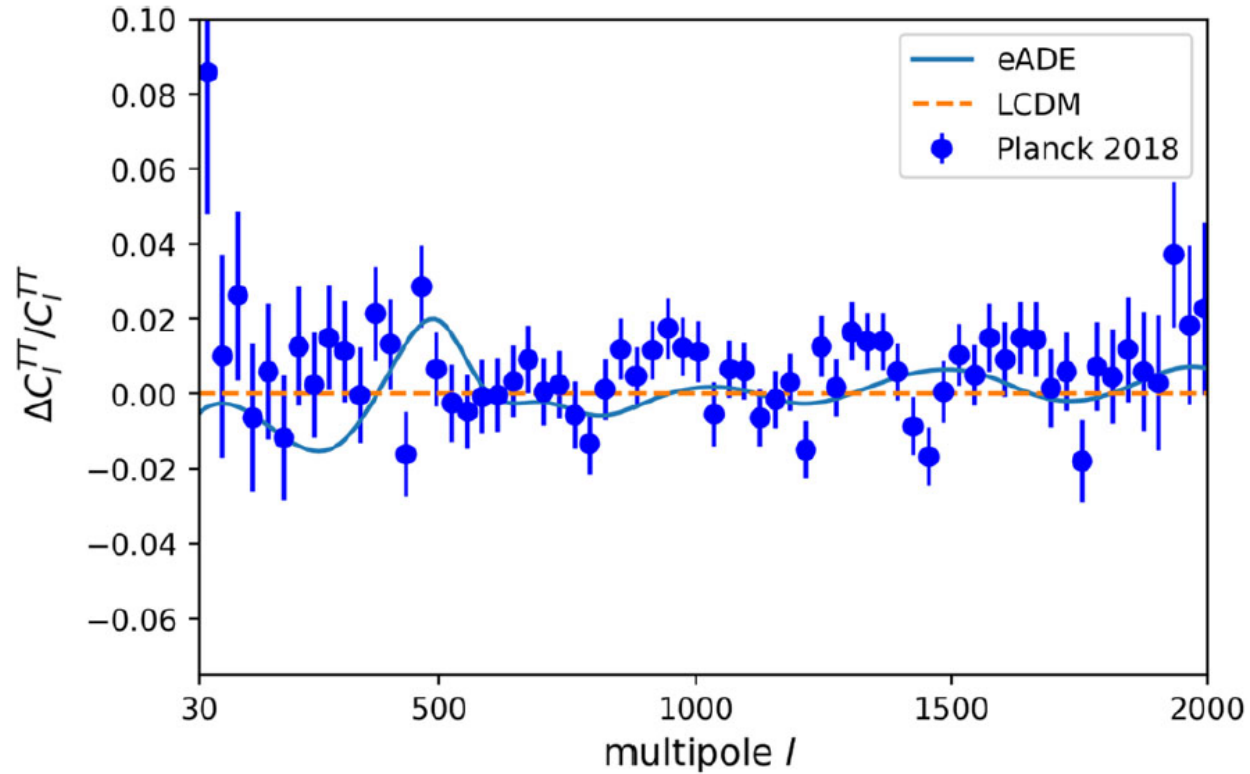
	EDE ( $n=2$ )	ADE
$f_c$	$0.028^{+0.011}_{-0.016}$	$0.079 \pm 0.033$
$\text{log}_{10} a_c$	$-4.136^{+0.57}_{-0.013}$	$-3.50 \pm 0.15$
$H_0$	$70.3 \pm 1.2$	$70.20 \pm 0.88$



# Fitting result for the eADE model



# The difference in CMB power spectra



The eADE model is closer to the CMB data than LCDM, especially in the EE mode.

# Conclusion

- The eADE is a new dark fluid model with *exponential EoS* to *release the H0* tension effectively.
- eADE model has *less additional parameters*
- The eADE is *closer to the CMB observation* than LCDM.

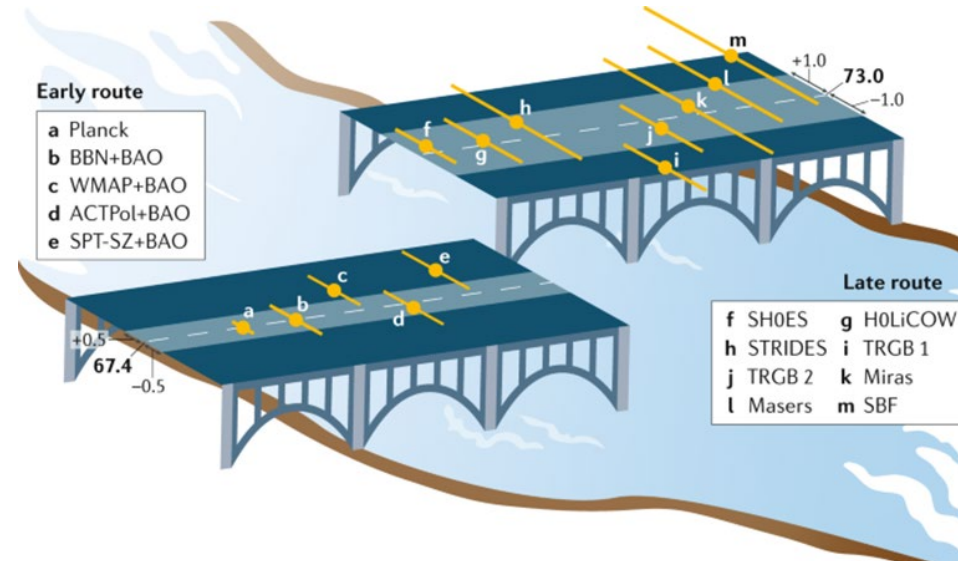
Thanks for your attention!





# Summary of recent $H_0$ values

<b>Cepheids</b>	<b><math>74.3 \pm 2.1</math></b>	<b>(2.8%)</b>	<b>[WLF+ 2012]</b>
<b>+ SNIa :</b>	<b><math>73.24 \pm 1.74</math></b>	<b>(2.4%)</b>	<b>[Riess+ 2016]</b>
	<b><math>73.52 \pm 1.62</math></b>	<b>(2.2%)</b>	<b>[Riess+ 2016]</b>



<b><math>\Lambda</math>CDM:</b>	<b><math>67.8 \pm 0.9</math></b>	<b>(1.3%)</b>	<b>[Planck 2015]</b>
<b>+ polarization</b>	<b><math>66.93 \pm 0.62</math></b>	<b>(0.9%)</b>	<b>[Planck 2016]</b>
	<b><math>67.4 \pm 0.5</math></b>	<b>(0.7%)</b>	<b>[Planck 2018]</b>

# In the next

- What is the difference between EDE, ADE, eADE model ?
- My model: the eADE model and its fitting result.
- Conclusion



- Release Ho REASON
- TU

$$r_s = \int_0^{t_\star} \frac{dt}{a(t)} c_s = \int_{z_\star}^{\infty} \frac{dz}{H(z)} c_s$$

# The difference between EDE, ADE, eADE model

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